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# VLBI Scale Effects

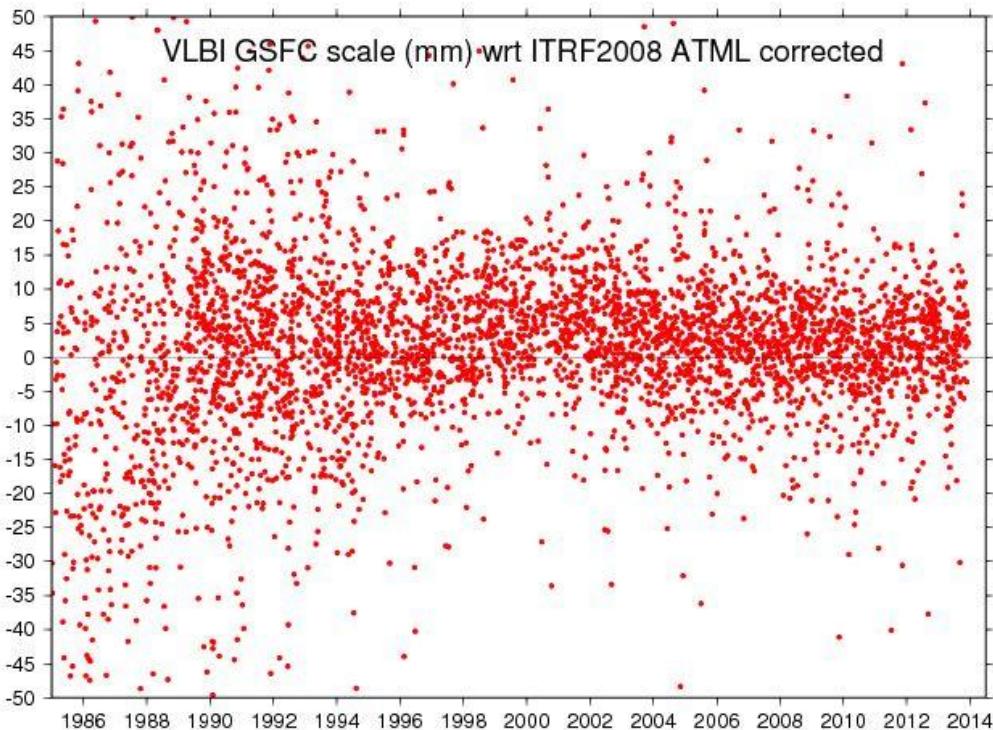
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NVI Inc.

Unified Analysis Workshop  
Pasadena – June 27, 2014

## Systematic Errors Contributing to VLBI Scale

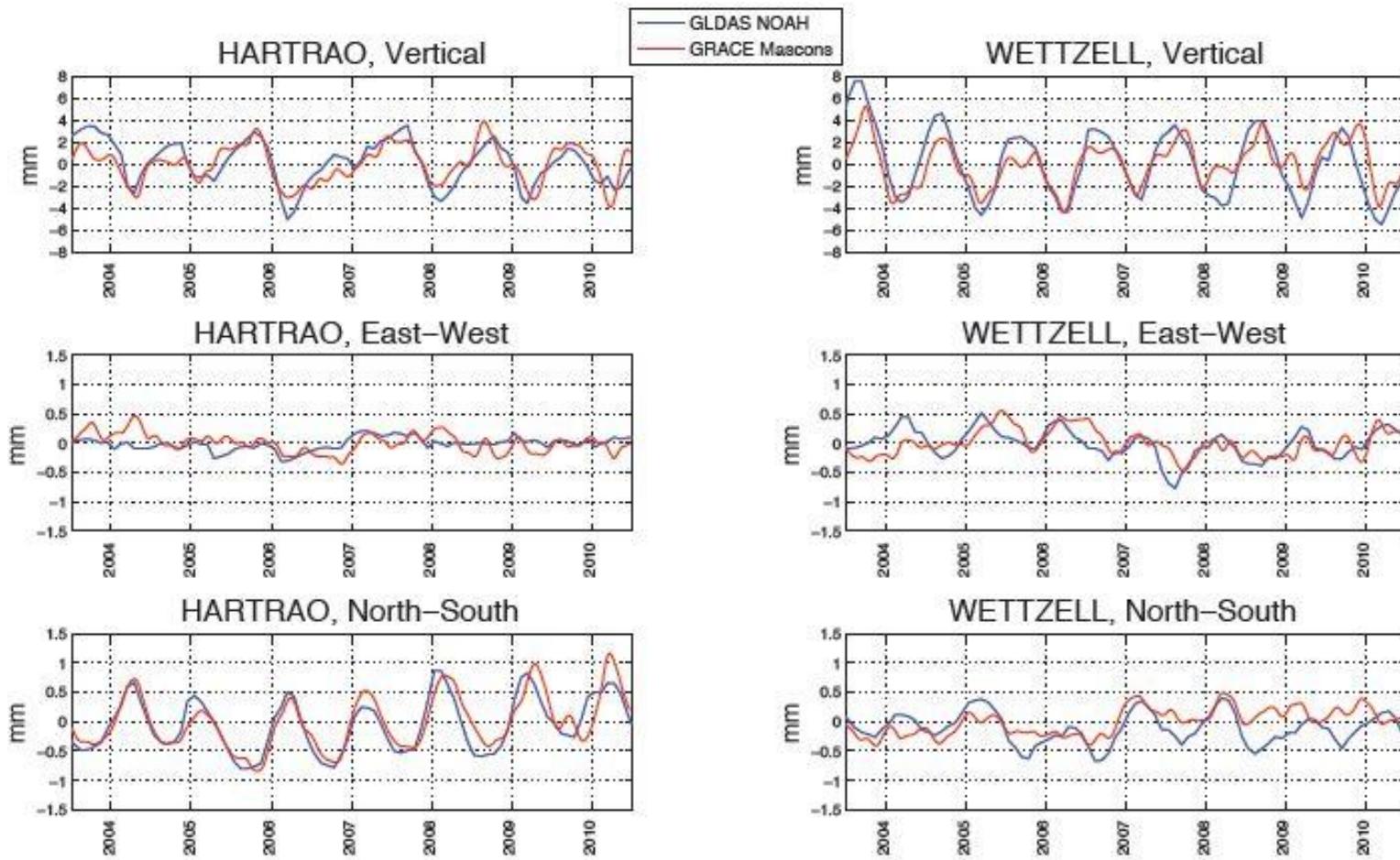
- Pressure loading and hydrology loading
- Antenna gravitational deformation
- Atmospheric delay modeling
- Radio source structure

# VLBI Scale Series



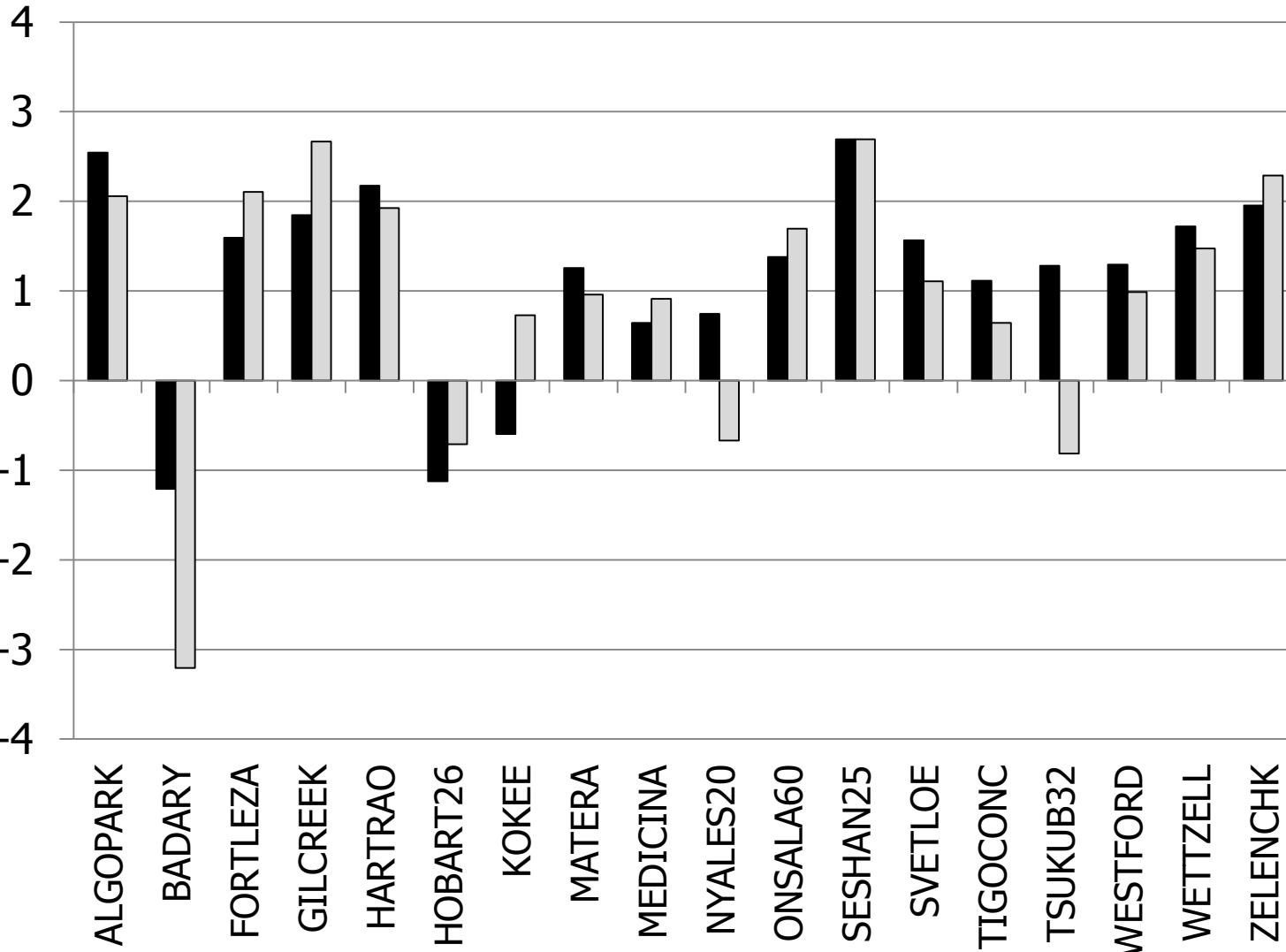
VLBI daily series  
relative to ITRF2008  
GSFC2011b sinex  
weighted mean  
difference = 1.98 mm  
(0.33 ppb)  
(from Z. Altamimi)  
ITRF2008 paper:  
(1980-2008 data)  
(Altamimi et al.)  
=>  $0.53 \pm 0.10$  ppb

# Hydrology Loading



# Hydrology Loading

Vertical WRMS Reduction (mm)



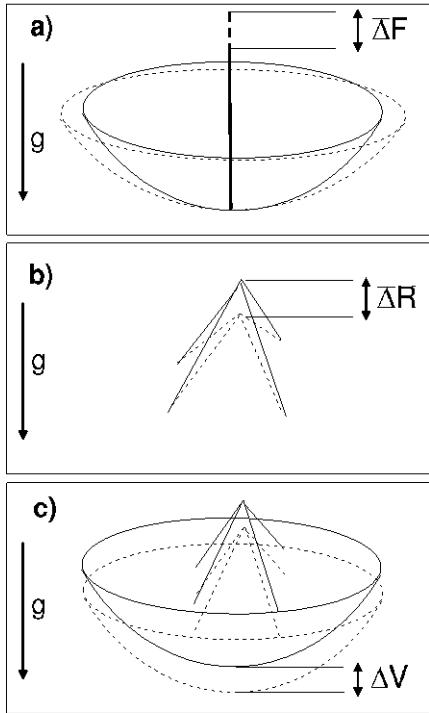
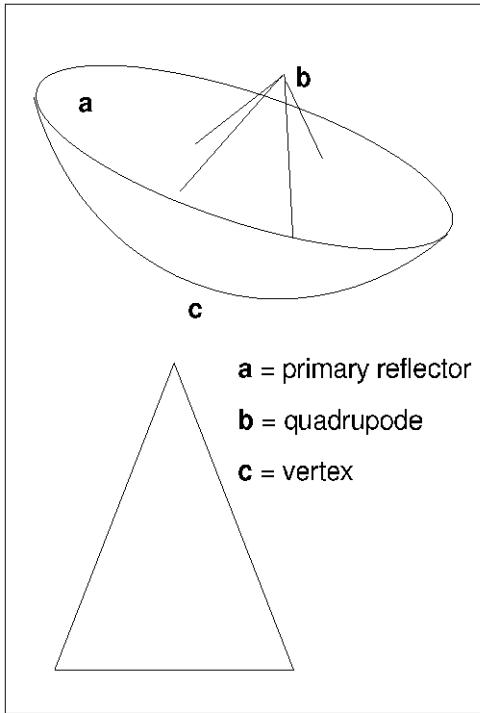
# Loading



			Annual	
	Offset ppb	Rate ppb/yr	Cosine ppb	Sine ppb
No Loading	0.44 $\pm 0.03$	0.005 $\pm 0.003$	-0.15 $\pm 0.02$	-0.29 $\pm 0.02$
Atmos Loading	0.44	0.001	-0.19	-0.32
Atmos+Hydro Loading	0.30	-0.007	-0.03	-0.01

Estimates are relative to ITRF2008. Data period 1980-2008.

# Gravitational Deformation



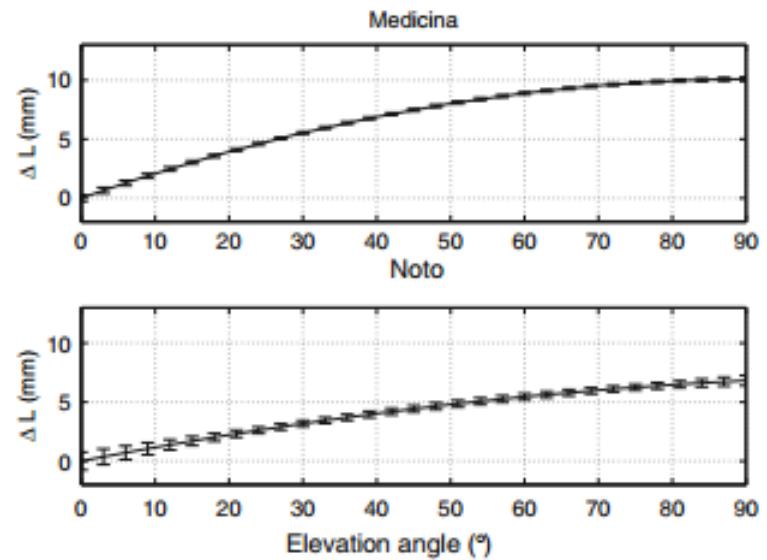
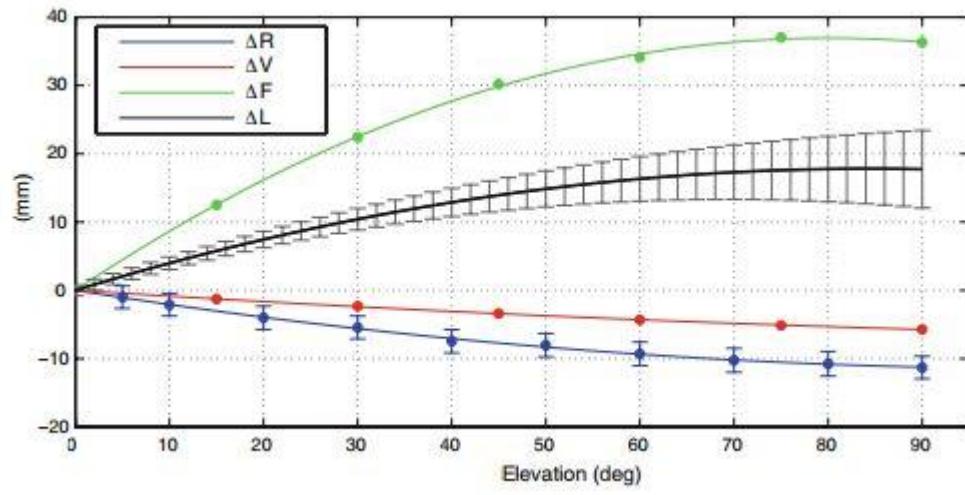
Clark and Thomsen (1988) model for signal path delay depends on variations of

- 1) focal length
- 2) vertex position
- 3) receiver position

$$\Delta L(e) = \alpha_F \Delta F(e) + \alpha_V \Delta V(e) + 2\alpha_R \Delta R(e)$$

- Coefficients depend on dimensions and structure of antenna
- The functions F, V and R have to be measured for each antenna

# Gravitational Deformation



- Measurements of Noto and Medicina (Sarti and Abondanza, 2009,2010)  
laser scanner (F)+ terrestrial survey (R)+ finite element model (V)
- Model of deformation from Clark and Thomsen (1988)  
XY mount antenna at Fairbanks (26 meter diameter)

$$\Delta L(e) = - 2.4 (1 - \sin(e)) \text{ mm}$$

# Gravitational Deformation

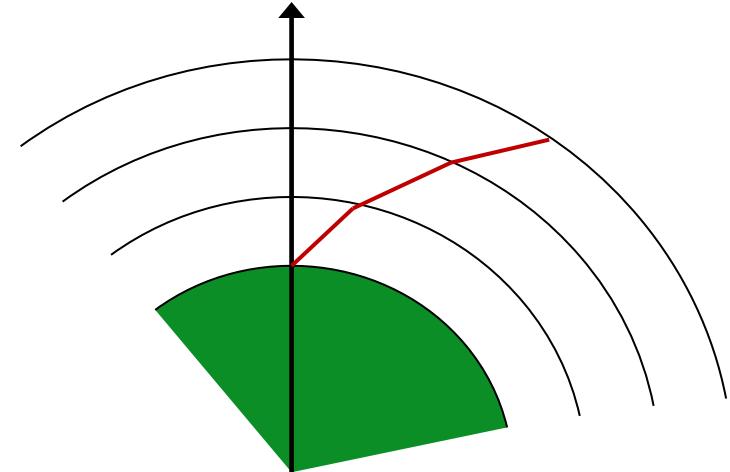


	Offset ppb	Rate ppb/yr
No Model	0.44 ± 0.03	0.005 ± 0.003
Medicina Model	1.24	0.014
Noto Model	0.89	0.011
Fairbanks Model	0.75	0.01

- Scaled each model delay ( $\sim \text{Diam}^2$ ) to the antenna diameter of each antenna in the solution.
- Estimates are relative to ITRF2008. Data period 1980-2008.

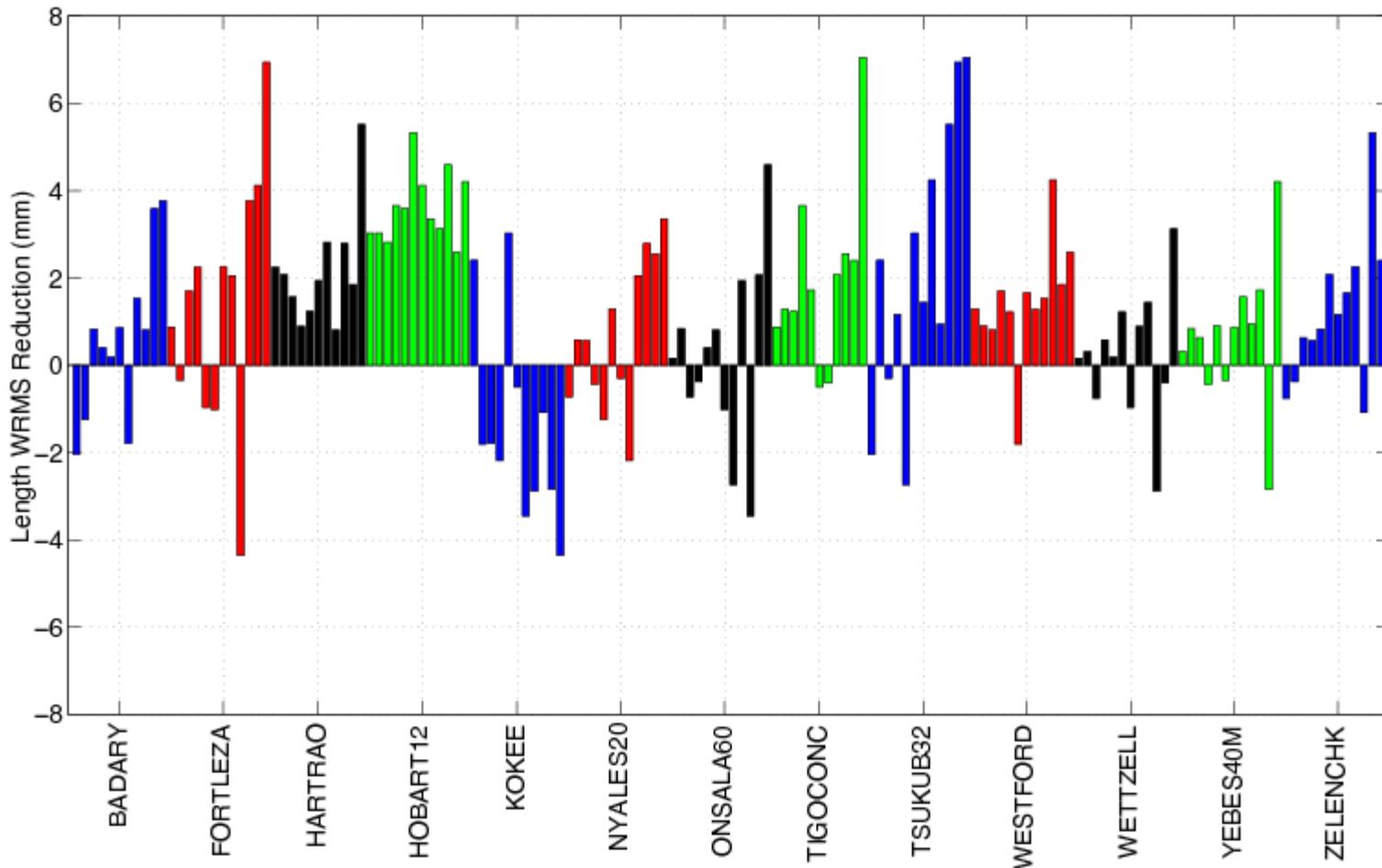
# Troposphere Raytracing

- Compute total (dry+wet) delays and wet mapping function from numerical weather model for each VLBI observation
- Weather model is the NASA/GSFC GEOS 5.9.1
  - parameters: pressure, temperature, specific humidity, geopotential height
  - time resolution: 3 hours
  - horizontal resolution:  $0.5^\circ \times 0.625^\circ$  ( $\sim 50$  km)
  - vertical resolution: 72 levels
- Refractivity along raypath is determined by interpolation of the 4D refractivity field
- Use piecewise linear approach to compute raytraced delays
- Constrain propagation of the ray to a plane of constant azimuth (to minimize computation time)



# CONT11 Baseline Lengths

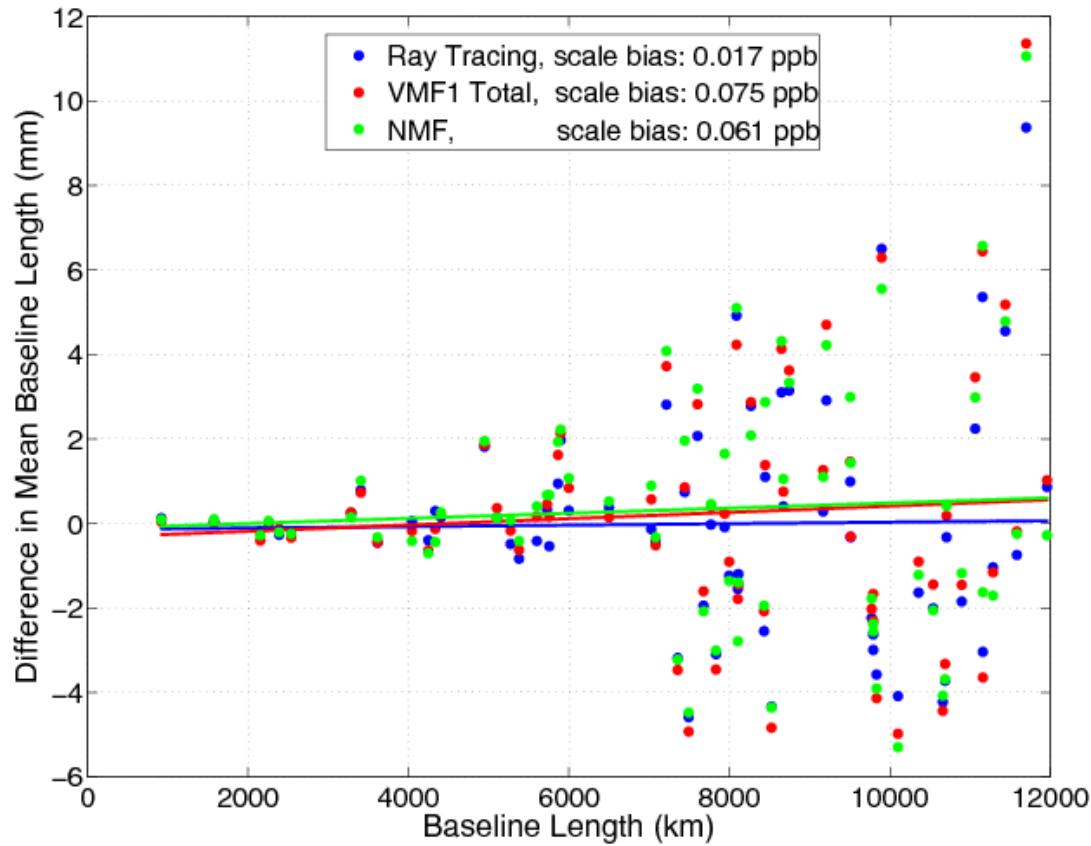
Improvement Relative to VMF1



- Ordered by baseline length for each site

# Troposphere Scale Bias Error

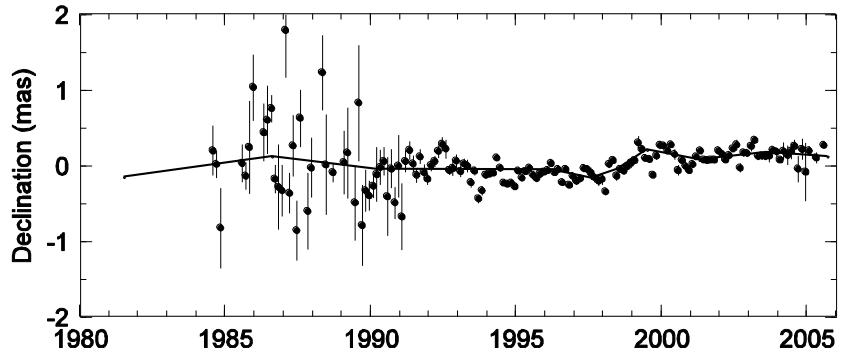
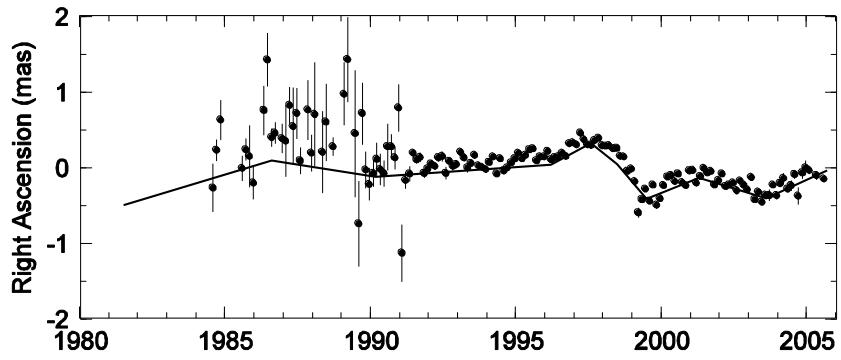
Elevation cutoff test: Difference 5° and 12° solutions CONT11 (2011)  
=> measure of atmosphere model error



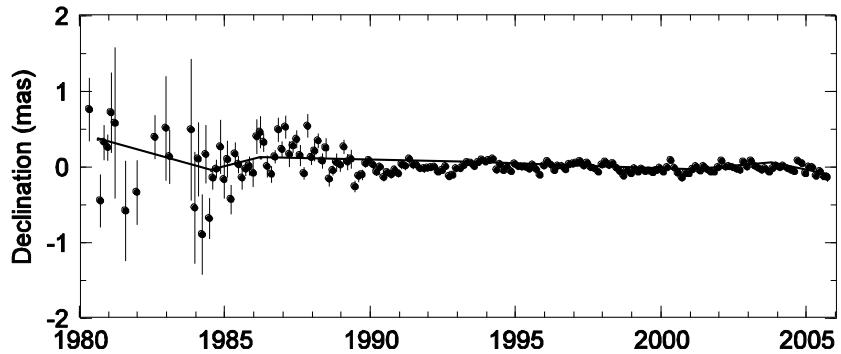
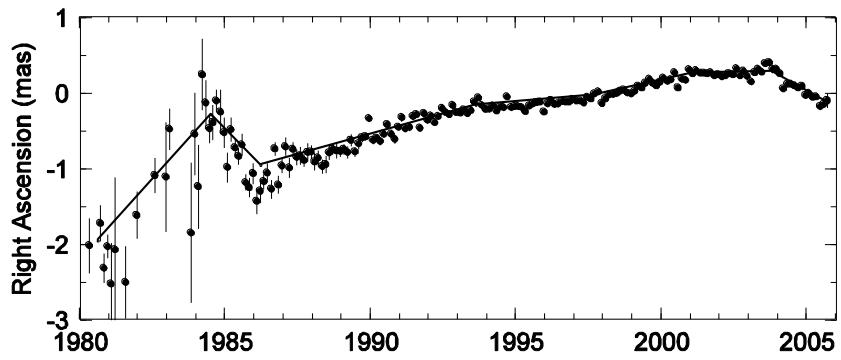
Raytrace: 0.017 ppb   VMF1: 0.075 ppb   NMF: 0.061 ppb

# Radio Source Instability

- Radio source position estimates can have large rates or even nonlinear variation
  - Identified sources with unstable position time series from among the most frequently observed (geodetic) sources



Radio source 2145+067



Radio source 4C39.25

- Modeled the position variation of unstable sources either by
  - (1) estimating global spline parameters to fit the variation
  - or (2) estimating positions for each 24-hour observing session

Effect of radio source instability =>

1) Spline	$-0.02 \pm 0.01$ ppb	$0.004 \pm 0.002$ ppb/yr
2) Local	$-0.02 \pm 0.02$ ppb	$0.008 \pm 0.002$ ppb/yr

# Scale Error Budget

Error Source	Annual Cos	Annual Sin	Rate ppb/yr	Bias ppb
Gravitational Deformation	--	--	-0.005 to -0.009	-0.78 to -0.31
Hyd Load	-0.16	-0.31	0.008	0.14
Atm Load	0.04	0.03	0.004	0
Atmosphere	--	--	0.010	0.08
Radio source	---	--	-0.006	0.02
ITRF2008	-0.16 ± 0.02	-0.30 ± 0.02	0.025 ± 0.010	0.53 ± 0.10